

# The Delineate Distribution and Quantity of Gas Production Optimization Using Linear Programming on Reverse Fishbone Diagram

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## ABSTRACT

This paper presents the outcome of our research on the delineate distribution and quantity of gas production optimization using linear programming on reverse fishbone diagram in an oil field. On using the reversed fishbone model to portray produced gas distribution and quantity, the model accurately describes the Gas Production Company under study. A production line on arrival to the production facility is routed into two phased production Separator, where gas is separated and formed the primary source for compressed gas. After compression with a metered volume, the pressurized gas is shared based on production demand and dynamics. For planning purposes, the strategic gas plan for Nigeria (2004) pegs a conservative gas cost per one Mcf between less than \$0.25 to about \$0.70 (source: The National Gas Strategy Plan for Nigeria (2004), joint UNDP World Bank Energy Sector Management Assistance Programme (ESMAP). The gas production cost of \$0.5 will be adopted for this research work. This research will adopt the Nigerian National Petroleum Company (NNPC) natural gas price of \$2.501 of 15<sup>th</sup> March, 2021 over USA (Henry Hub) average gas price of \$2.675 per mcf. Then, the alternative fuel gas cost (diesel running cost) per day was calculated as per dayper day

**KEYWORDS:** The Delineate Distribution, Production Optimization, Production Channeling Linear Programming, reverse fishbone diagram, Petroleum Product Recovery, Orifice Plate Size.

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## I. INTRODUCTION

The development in the world today has created a massive rise in the demand for energy. Over the years there has been a drastic increase in the consumption rate of energy. Global activities like manufacturing processes and technology boost are dependent on energy for their day-to-day activities (Aalo, 2019). So far energy consumption has been centered on fossil fuels of which natural gas makes up 21% of the world's energy supply. This massive and growing demand for natural gas have brought with it some major problems ranging from over-dependence to climatic change in the environment as a result of increased concentration of Green House Gas (GHG) being flared in the atmosphere during production.

The reverse fishbone diagram is an analysis tool that provides a systematic way of looking at effects and the causes that create or contribute to those effects. The approach combines brainstorming and a concept map. The process has four major steps: identifying the problem; working out the major factors involved; identifying possible causes and analyzing the cause and effect diagram. The structure provided by the diagram helps team members think in a very systematic way. Some of the benefits of constructing a reverse fishbone diagram are that it helps determine the root causes of a problem or quality characteristic using a structured approach, encourages group participation and utilizes group knowledge of the process, identifies areas where data should be collected for further study (Masoud, 2011).

The ultimate goal of virtually all effort spent on gas production is to devise an optimal strategy to develop, manage, and operate the production of such gas which creates a need for a process, or methodology of making the process perfect, functional, or effective as possible called optimization (Pengju, 2003). In optimization of small systems like a single well or mild pattern creation simple nodal analysis may be adequate

but large complex systems like gas production demand a more sophisticated optimization approach which will be done in this project by the use of linear programming on reverse fishbone diagram.

As the upsurge in the demand for energy continues to increase, natural gas despite its massive demand has not till recently been heavily faced with loads of challenges which has thrown the oil and gas industry into transformational times and has reflected in its deep price drop resulting from trade wars between production countries to other factors. With these changes, the industry is faced with several challenges in achieving its goals of efficient and environmentally responsible operations, capital cost reduction and profit maximization. This adds up to the need for optimization in gas production.

### **1.1 Statement of the Problem**

The activities of multinational oil companies have their main objective as the production of oil and gas for improved economic development. These activities when not properly organized tend to become a major source of environmental degradation culminating into deprivation of sources of livelihood.

This degradation is as a result of intense global warming derived from flared gases. The advent of excessive flared gas and a knowledge of the proper use of some of the flared gas, gave rise to the utilization of part of the gas for reinjection and compression, especially when in an associated form. The need therefore arises to properly estimate the rate at which these gaseous components are distributed.

The technique for this estimation utilizes a linear programming approach. This approach can predict the quantities of gas at a particular time, at a particular chain of distribution on a Reversed Fishbone Diagram.

### **1.2 Objective of the Study**

The objective of this research work is to delineate distribution and quantity the reversed fish bone model

## **II. MATERIALS AND METHODS**

### **2.1 Description of the Facility**

The facility is provided with three parallel production trains into which production is channeled. Each train is provided with a separator and pumps that deliver the oil through pipeline to treatment and processing points where the gas is now channeled to the inlet drum.

The gas is made to flow into four parallel low-pressure compressor units, each with two stages. At this unit, the gas is then dehydrated with tri-ethylene glycol contactor after partial compression. Some of the gasses are diverted to a supply gas pipeline while the rest is compressed in two parallel two-stage High Pressure (HP) compressor units. The product of the high-pressure compression is the interest of this work as it is further used for sales gas; injection/Gas lift; for other uses including domestic and may be flared if not used adequately.

### **2.2 Gas Gathering and Separations**

Gas distribution headers and its associate Separation equipment of the case study facility forms the preliminary material for this research. The gas route is observed to have a single source gas input from the satellite platform with option of alternate support route from a nearby independent facility. The gas is routed from an external/satellite platform to a manned production platform. On arrival the gas passed through the gas gathering headers and is lined up into a Separator. On condition that the inflow is expected to be high, another Separator is commissioned to handle the fluid influx. The aforementioned equipment separates the input hydrocarbon fluid into gas and liquid.

Plates 1 and 2 shows the gas gathering headers, primary and secondary gas separation prior to gas compression. It should be noted that the scrubbed liquid is evacuated off the vessels by its discharge pumps.



- i. Compressed Sales Gas
- ii. Reinjection Gas
- iii. Gas Lift Gas
- iv. Fuel and Seal Gas.

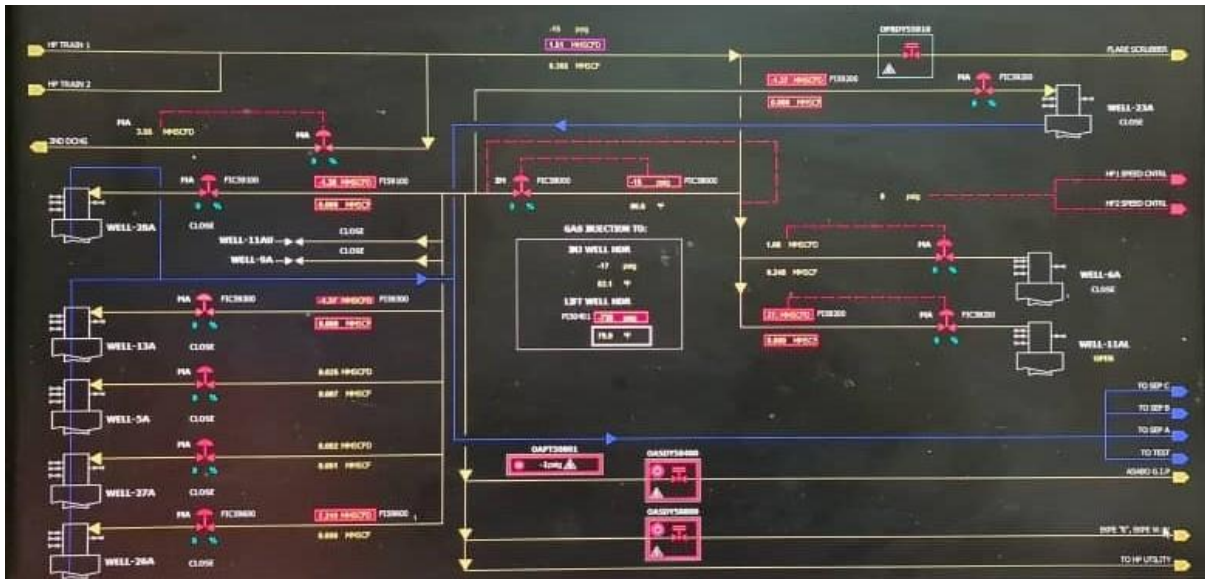


Plate 3: Compressed Gas Distribution Headers

**2.6 Constraint Equations**

This is the amount of gas which will be produced before compressed gas distribution can occur and is taken as C at a cost of

$$\frac{p+q+r}{3} = sC \tag{1}$$

where

- p = net profit of compressed sales gas
- q = net profit of lifting gas
- r = net profit/loss of reinjection gas
- 3 = total number of variables observed
- s = cost per unit of total compressed gas
- C = constraint

The constraint equation for the cost of compressed point becomes:

Cost on A + Cost on B + Cost on D = cost on compressed gas point.ost on A + Cost on B + Cost on D = cost on compressed gas point.

as

$$fA + gB + hD = sC \tag{2}$$

where

- f = cost of A
- A = Sales gas
- g = cost of B
- B = Gas lift gas
- h = cost of D
- D = Reinjection gas

The second constraint is the storage areas (total provided)

$$A + B \leq \text{capacity of tank, store if not flared} + B \tag{3}$$

$$D \leq 0 \tag{4}$$

Non-Negativity restriction

$$A \geq 0, B \geq 0, D \geq 0 \tag{5}$$

The Linear Programming graph is plotted for constraints to determine A; B& D. A, B& D, values are put in the objective function, (Max Z)



where Max Z = maximize overall profit.

### 2.7 Theory of The Reversed Fishbone Diagram

This is a schematic model which hitherto was used as an effect to cause model but will be used in this work as a single input, multiple output system. The reversed fishbone diagram is a direct fallout of the fishbone diagram which is also seen as multiple input single output system.

The single input system in this case is contrived to be the highly pressured well head crude, which on pre-processing liberates Natural gas, after the removal of Natural Gas Liquids (NGLs). The natural gas constitutes or is modelled into the multiple output systems viz: compressed gas: injection gas for gas lifting and flaring gas. The compressed gas is stored according to the capacity of storage available and are sent out to various distribution lines.

The gas lifting components are stored and released into well casing to lift oil from low producing or non-producing wells. The utilization of the gas lifting component is premised on the principle of solubility of the mixture, thereby increasing the fluidity and flow of crude. Another principle is the use of non-soluble gas to increase underground pressure and flow head of the crude. The method notwithstanding, the gas friction pressure increases till crude flow reduces. This becomes a constraining factor for gas lift.

Excess gas that cannot be compressed or stored, becomes flared, not minding the restriction in form of tax placed on flared gas. This simple reversed fishbone diagram gives a soft landing for the application of linear programming to determine

- i. How cost effective the processes are
- ii. How to maximize profit
- iii. The point at which flaring of gas is inevitable.

### 2.8 Reversed Fishbone Analytical Steps

The single input system is the wellhead crude gas. The quantity is defined and may also include some NGLs. The cost equivalent is also analyzed.

The next step is to analyze the compressed sales gas (A), the cost of production (P) and selling price (F) are also noted.

The gas lifting gas component (B) will be considered. The cost of this gas is given as (q) and the selling price (g). The selling price of the gas lifting component is determined by finding the volume difference between the application of the gas lifting without the gas lifting. The equivalent cost of this price is the selling price.

The end product is determined by whether an excess exist or not and will be used as a constraint in the linear programming model.

#### To formulate

- i. Identify the decision variable
- ii. Write the objective function
- iii. Mention the constraints
- iv. Explicitly state the Non negativity restriction.

Since the amount of gas can be qualified in volume and associated cost attached then the objective function is as follows:

(A)

If  $1\text{m}^3$  of compressed sales gas cost #10 and

(B)

$1\text{m}^3$  of gas lift gas cost #20

(D)

$1\text{m}^3$  of reinjection gas cost #10

Then the total profit (z) could be maximized(max) by the equation

$$\text{Max (Z)} = 10A + 20B + 10D \quad \text{ax (Z)} = 10A + 20B + 10D \quad (6)$$

In the event that the gas produced exceeds compression capacity and therefore requires to be flared at an extra flaring cost of #15 per cubic meter of compress gas.

Let the maximum amount of gas that compression system can conveniently contain and handle before allowing extra flaring be  $2000\text{m}^3$ , then the constraint equation will be

$$30A + 20B + 10D \leq 2000 \quad 10A + 20B + 10D \leq 2000$$

(7)

Formulating the problem into a mathematical model produces gas that could be stored and/or flared.

Let selling price of A = P

B = Q

$$D = R$$

$$\text{Max (Z)} = PA + QB + RD \quad \text{ax (Z)} = PA + QB + RD$$

roduced is constrained or limited by factors.

The decision variables: that determine output, are the variables P, Q & R.

The objective function: could be maximizing profit and reducing flaring.

Constraints: limit the values of the decision variables.

Non-Negative Restriction; decision variable should take > 0 value.

**Table 1: Revenue and Cost Models**

Models	Revenue	Cost	Net Profit
A	P	F	P
B	Q	G	Q
D	R	H	R
<b>TOTAL</b>			

**Given that:**

- i. Natural gas price = \$2.501 per kcf
- ii. Brent oil = \$68.93 per barrel
- iii. WTI oil = \$65.4 per barrel (source: <https://nnpcgroup.com/pages/home> on 15<sup>th</sup> March 2021)
- iv. Crude production on 30<sup>th</sup> Jan., 2020 = 5.142kb.

Tables 1 and 2 depict the cost of Natural gas in the past 4 years. This research will adopt the Nigerian National Petroleum Company (NNPC) natural gas price of \$2.501 of 15<sup>th</sup> March, 2021 over USA (Henry Hub) average gas price of \$2.675 per mcf.

**Table 2: Price of U.S. Liquefied Natural Gas Import from Nigeria (Dollar per Thousand Cubic Feet. Source: U.S. Energy Information Administration (www.eia.gov))**

Gas Price (mcf)	Year				Average
	2017	2018	2019	2020	
Price in US Dollar	6.52	8.84	5.56	3.5	6.105

**Table: 3 Price of Liquefied Natural Gas(Dollar per Thousand Cubic Feet. Source: World Bank Commodity Pink Sheet)**

Gas Price (mcf)	Year				Average
	2017	2018	2019	2020	
U S (Henry Hub)	2.96	3.16	2.57	2.01	2.675
Europe	5.72	7.68	4.8	3.24	5.36
Liquefied Natural Gas Japan	8.61	10.67	10.56	8.31	9.5375

For planning purposes, the strategic gas plan for Nigeria (2004) pegs a conservative gas cost per one Mcf between less than \$0.25 to about \$0.70 (source: The National Gas Strategy Plan for Nigeria (2004), joint UNDP World Bank Energy Sector Management Assistance Programme (ESMAP). The gas production cost of \$0.5 will be adopted for this research work.

Using average field data for year 2020 on table 5:

$$\text{Max (Z)} = (P - f)A + (Q - g)B + (R - h)D \quad \text{Dax (Z)} = (P-f)A + (Q-g)B + (R-h)D$$

$$= ((14.21 \times 2501) - (14.21 \times 1))A + ((5.97 \times 35.85) - (5.97 \times 1))B + ((3.37 \times 0) - (3.37 \times 1))D$$

$$= (35,539.21 - 14.21)A + (214.025 - 5.97)B + (0 - 3.37)D$$

$$35,539.21 - 14.21A + 214.025 - 5.97B + 0 - 3.37D = 0 \quad (8)$$

On the same year, the average gas production based on streaming wells = 31.97Mscf

It implies that for year 2020,  $A + B + D = 31.97\text{Mscf(Avg)} + B + D = 31.97\text{Mscf(Avg)}$

where

$A : B : D = 2.4 : 1 : 0.6$  average gas production data.

where

$$A \leq 2.4 \quad (3.15)$$

It implies that B is to D as 2 is to 1 approximately.

$$B : D \leq 2 : 1 \quad (3.16)$$

Multiplying both sides by D

$$B \leq 2D \quad (3.17)$$

Where the slack capacity due to well downtime (on high water rate, high sand production and pipeline rupture etc) equals to 22.7Mscf.

The general inventory constraint, implies that

$$A + B + D = 55.0\text{Mscf} + B + D = 55.0\text{Mscf}$$

## 2.9 Reversed Fishbone Redistribution Modes

Applying the RFB model on the case study, four modes were obtained as follows:

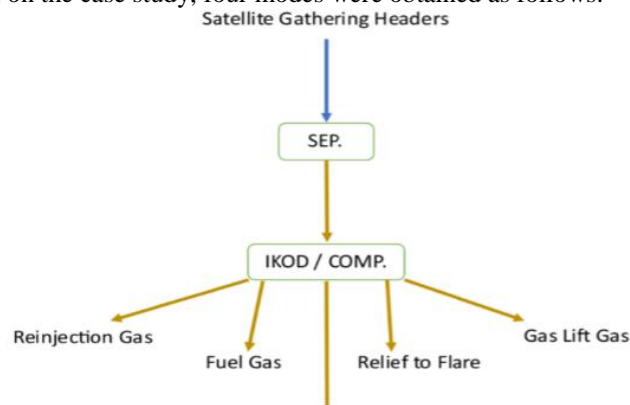


Figure 1: Normal Gas Production Network

Figure 1: Illustrates an additional gas channel. It is a bi-directional pipeline design to either boost source gas for compression or export gas to a nearby facility.

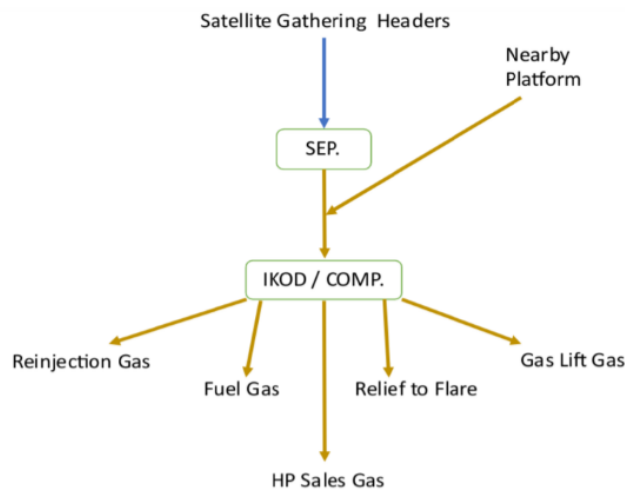
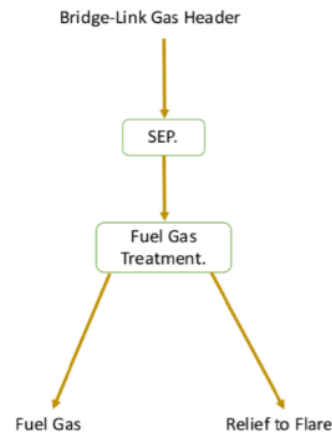


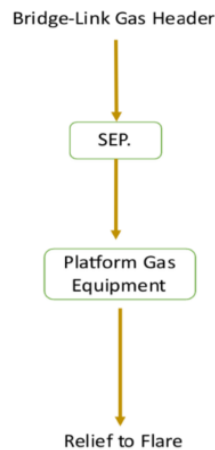
Figure 2: Alternate Support Gas Production Network

Figure 3. explains an alternate gas line-up, on condition that the facility needs only fuel gas to runs its equipment. Blackstart condition indicates a total plant shutdown mode and has a need of a fuel gas lined-up only for end users, for example Gas Power Generator. The main aim is to supply fuel gas, however the relief to flare is unavoidable so as to maintain operating pressure in the lined-up equipment.



**Figure 3: Blackstart Fuel Gas Production Network**

There are occasions where a planned sectional or overall turnaround maintenance is carried out in the facility. In these period vessels and pipeline are seldom exposed to atmospheric condition hence the need to evacuate oxygen from the production equipment prior to production startup. Figure 4. shows a distribution mode used for vessel and pipeline purging.



**Figure 4: Purge Gas Line-Up**

### 2.10 Data Collection Source

This research derived its data from SUCCESS production platform field raw data. The Company majors is petroleum extraction and components (oil and gas) production. The gas production component and its optimization were applied in this study.

## III. RESULTS AND DISCUSSION

### 3.1 Field Data Analysis 2019

Raw field data in Table 4 represent values obtained between January to December 2019. To optimize gas production, these values are needed for computation.



**Table 4: Gas Production and Utilization Field Data 2019**

Gas Utilization (mcf/d)	Dates								Avg
	5-Feb	6-Feb	12-Apr	13-Apr	7-Aug	8-Aug	21-Oct	22-Oct	
SUCCESS Gas to Separator	43	43.3	44.3	43.7	34.1	34.4	26.9	23.1	36.60
From Nearby Platform	0	0	0	0	0	0	8.4	19	3.43
SUCCESS Compressed gas	33.3	33.7	34.7	34.1	28	28	27.3	33	31.51
Export/Sales to nearby Platform	7.9	7.9	6	5	0	0	7.6	9	5.43
SUCCESS gas lift gas	25.33	25.74	26.41	29.15	11	8.89	11.2	16	19.22
SUCCESS storage/reinjected gas	0	0	0	0	17	19.1	8.5	8	6.58
SUCCESS fuel gas	8.74	8.74	8.74	8.74	5.5	5.5	7.7	8.74	7.80
SUCCESS flare gas	1	0.9	0.9	0.9	0.6	0.9	0.3	1.4	0.86

### 3.2 Field Data Analysis 2020

Raw field data below represent values obtained between January to December 2020. To optimize gas production, these values are needed for computation. It will be use to compute and deduce into the constraint equation.

**Table 5: Gas Production and Utilization Field Data 2020**

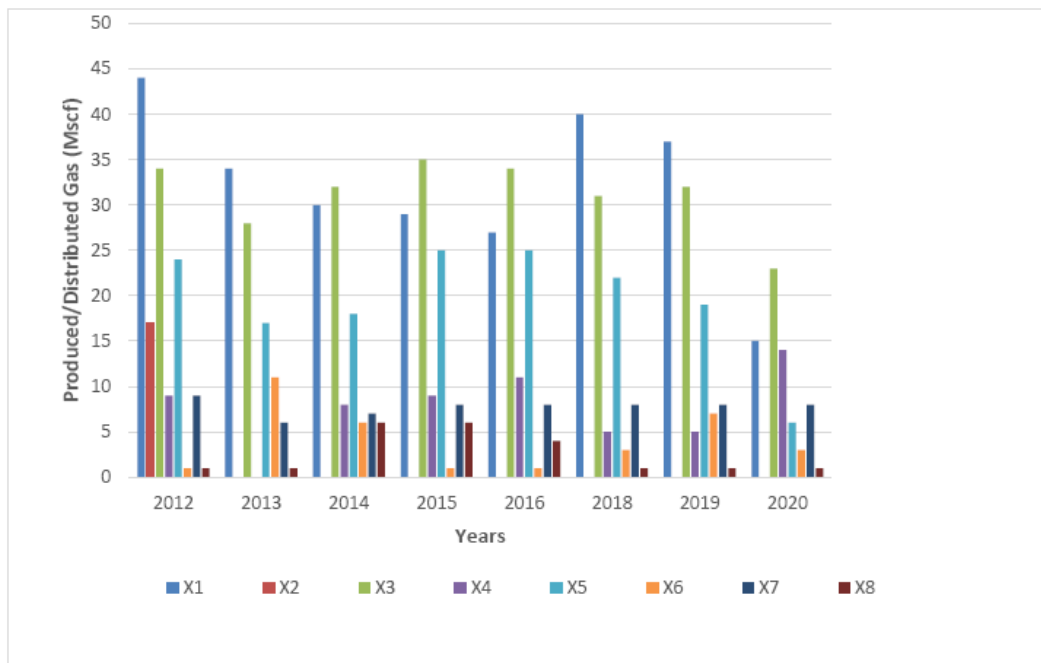
Gas Utilization (mcf/d)	Dates								AVG
	10-Jan	18-Jan	5-Mar	6-Mar	8-Mar	28-Jul	13-Dec		
SUCCESS Gas to Separator	9.1	8	17	17.2	20.9	20.6	15.3	15.44	
From Nearby Platform	21.9	20.6	22.1	22.3	3.9	4.6	20.3	16.53	
SUCCESS Compressed gas	21.4	20	29.5	29.9	18.5	19	26	23.47	
Export/Sales to nearby Platform	18.9	19.9	21.4	21.4	3.4	4.5	10	14.21	
SUCCESS gas lift gas	2.5	0.1	8.54	8.54	3.76	6.31	12.03	5.97	
SUCCESS storage/reinjected gas	0	0	0	0	11.5	8.1	4	3.37	
SUCCESS fuel gas	8.7	7.7	8.7	8.7	8.7	6.3	8.7	8.21	
SUCCESS flare gas	0.8	0.9	0.9	0.9	0.8	0.9	0.9	0.87	

### 3.3 Data Optimization and Result

Raw field data in Table 6 represent average values obtained between Year 2012 to 2020. These values were used for optimization computation.

**Table 6: Average Yearly Gas Production and Utilization Field Data**

Gas Utilization (mcf/d)	Year							
	2012	2013	2014	2015	2016	2018	2019	2020
Gas to Separator	44	34	30	29	27	40	37	15
From Nearby Platform	0	0	16	20	20	0	3	17
Compressed gas	34	28	32	35	34	31	32	23
Export/Sales to nearby Platform	9	0	8	9	11	5	5	14
Gas lift gas	24	17	18	25	25	22	19	6
Storage/reinjected gas	1	11	6	1	1	3	7	3
Fuel gas	9	6	7	8	8	8	8	8
Flare gas	1	1	6	6	4	1	1	1



**Figure 5: Average Gas Production and Distribution Field Data Per Year**

#### 4.0 CONCLUSION

In the onset of this research, objective is to use the reversed fish bone model to delineate distribution and quantity.

On using the reversed fishbone model to portray produced gas distribution and quantity, the model accurately describes the Gas Production Company under study. A production line on arrival to the production facility is routed into two phased production Separator, where gas is separated and formed the primary source for compressed gas. After compression with a metered volume, the pressurized gas is shared based on production

demand and dynamics. The gas production revealed a single source intake and multiple distribution routes, hence the reversed fishbone modelling.

The importance of gas optimization of the produced wells in attaining the desired production goals cannot be overstated. Production goal include profit maximization and lost minimization.

With the application of data optimization tool to the field data, the following conclusion were pinched:

- i. Three parameters were tested over the period of eight years from field data obtained on a case studied.
- ii. Gas production has alternate routes which helps in evaluation of production routes, techno-economic performance, storage, and safety. Also, the gas production route could be in a more stable form and can be easily transported to the place of use.
- iii. Maximization of gas production could help in production and distribution chains to increase the pressure of natural gas by reducing its volume.

## REFERENCES

- [1]. Aalo, E. (2019). Design and Analysis of a 68MW Fuel Cell Power Plant. Project Report. Department of Mechanical Engineering, Rivers State University, Nigeria.
- [2]. Adejuge, A., & Onamade, B. (2014). Gas Flaring in Nigeria: Challenges & Investment Opportunities. Energy and Natural Resources Article. Strachan Partners.
- [3]. Amani, M., Ardestani, N. S., & Majd, N. Y. (2021). Utilization of Supercritical CO<sub>2</sub> Gas Antisolvent (GAS) for Production of Capecitabine Nanoparticles as Anti-cancer Drug: Analysis and Optimization of the Process Conditions. Journal of CO<sub>2</sub> Utilization. 46(2), 17-22.
- [4]. Alarcon, G. A., Torres-Monzon, C. F., Gonzalo, N., & Gomez, L. E. (2001). Global Optimization of Gas Allocation to a Group of Wells in Artificial Lift using Matlab. 23rd ASME Energy Resources Technology Conference and Exposition, February 5-7, Houston, Texas.
- [5]. Atilhan, S., Park, S., El-Halwagi, M. M., Atilhan, M., Moore, M., & Nielsen, R. B. (2021). Green Hydrogen as an Alternative Fuel for the Shipping Industry. Current Opinion in Chemical Engineering. 31(7), 19-26.
- [6]. Brikić, D. (2011). A Gas Distribution Network Hydraulic Problem from Practice. Petroleum Science and Technology. 29(4), 366-377.
- [7]. Buitrago, S., Rodríguez, E., & Espin, D. (1996). Global Optimization Techniques in Gas Allocation for Continuous Flow Gas Lift Systems. Paper presented at the SPE Unconventional Resources Conference, April 28<sup>th</sup> - May 1<sup>st</sup>, Calgary, Alberta.
- [8]. Caudle, B.H., & Mcleroy, P.G. (2019). Petroleum Production: Recovery of Oil and Gas. Britannica Encyclopedia. Retrieved from <http://www.britannica.com/technology/petroleumproduction>
- [9]. Czyzyk, J., Wisniewski T., & Wright S. J. (1999). Optimization Case Studies in the NEOS Guide in SIAM Review. Applied Mathematics. 41(1), 148 – 163.
- [10]. Das, P., Van Golden, I., Janssen, H., & Roels, S. (2015). Designing Uncertain Optimization Scheme for the Economic Assessment of Stock Energy Efficiency Measures. Journal of Building Performance Simulation. 10(1), 3-16.
- [11]. Dewi, R. R. (2021). The Evaluation by Passes Energy Based on in vitro gas Production Digestibility and Palatability. In IOP Conference Series: Earth and Environmental Science. IOP Publishing. 667, 12011.
- [12]. Eseduwo, F. S. (2014). Gas Flaring and Reinjection Policy-Making in Nigeria: Why Gas Reinjection Policies work in other Oil-producing Countries and Fail in Nigeria. Lambert Academic Publishing, Mauritius.
- [13]. Ehrhardt, K., & Steinbach, M. C. (2005). Nonlinear Optimization in Gas Networks in Modeling, Simulation and Optimization of Complex Processes. Proceedings of International Conference, High Performance Scientific Computing. March 10<sup>th</sup> to 14<sup>th</sup>, Hanoi, Vietnam. 139-148.
- [14]. Fang, W. Y., & Lo, K. K. (1996). A Generalized Well-Management Scheme for Reservoir Simulation, SPE Reservoir Engineering. 11(2), 116-120.
- [15]. Gerogiorgis, D. I., & Pistikopoulos, E. N., (2008). A Mixed Integer Optimization Strategy for Oil and Gas Production Planning. Centre for Process Systems Engineering, Imperial College London.
- [16]. Gohain, M., Hasin, M., Eldiehy, K. S., Bardhan, P., Laskar, K., Phukon, H., Mandal, M., Kalita, D., & Deka, D. (2021). Bio-ethanol Production: A Route to Sustainability of Fuels Using Bio-Based Heterogeneous Catalyst Derived from Waste. Process Safety and Environmental Protection. 146(5), 190-200.
- [17]. Guru, M. J. (2017). List of Natural Gas Processing plants in Nigeria. Retrieved May 20<sup>th</sup>, 2021 from [https://en.wikipedia.org/wiki/List\\_of\\_Natural\\_gas\\_processing\\_plants\\_in\\_Nigeria](https://en.wikipedia.org/wiki/List_of_Natural_gas_processing_plants_in_Nigeria) on 20<sup>th</sup> May, 2021.
- [18]. Huang, X., Qi, Z., Zhang, H., Yan, W., Chang, Y., Li, S., & Li, J. (2021). Effect of Stress-sensitive Permeability and Porosity on Production Performance in Water-soluble Gas Reservoirs. Journal of Energy Resources Technology, 143(11), 1-14.
- [19]. Ibrahim, M. T. (2007). Optimization of Gas Lift System in Varg Field. Faculty of Science and Technology, University of Stavanger, Norway.
- [20]. Igwilo, K. C., Okoro, E. E., Nwude, A. A., Mamudu, A. O., & Onuh, C. Y. (2018). A Review on Gas Well Optimization Using Production Performance Models – A Case Study of Horizontal Well. Open Journal of Yangtze Gas and Oil. 3(1), 57-67.
- [21]. Ishii, K. & Lee B. (1995). Reverse Fishbone Diagram: A Tool in aid of Design for Product Retirement. ASME Design Engineering Technical Conference and Computers in Engineering Conference, Design for Manufacturing Conference, August 18<sup>th</sup> – 22<sup>nd</sup>, Irvine, California.
- [22]. Izuwa N. C. (2017). Improving Natural Gas Distribution and Management in Nigeria. International Journal of Scientific & Engineering Research. 8(7), 330-334.
- [23]. Kanu, E. P., Mach, J., & Brown, K. E. (1981), Economic Approach to Oil Production and Gas Allocation in Continuous Gas Lift Problems, Journal of Petroleum Technology. 33(10), 1887–1892.
- [24]. Kraus, R. S. (1996). Oil Exploration and Drilling: Exploration, Drilling and Production of Oil and Natural Gas. ILO Encyclopedia of Occupational Health and Safety. 4<sup>th</sup> Edition. Chapter 75.
- [25]. Krishnamoorthy, D., Fjalestad, K., & Skogestad, S. (2019). Optimal Operation of Oil and Gas Production using Simple Feedback Control Structures. Control Engineering Practice Journal. 91(12), 104-107
- [26]. Lewis, C. (2018). Linear Programming: Theory and Application. University of Houston, Texas. 43-46.

- [27]. Loyer, C. (2009). The Fishbone Diagram and Reversed Fishbone Diagram Concept. PEX Process Excellence Network, Orlando, Florida.
- [28]. Luo, X., Zheng, P., Gao, K., Wei, B., & Feng, Y. (2021). Thermo-and CO<sub>2</sub>-triggered Viscosifying of Aqueous Copolymer Solutions for Gas Channeling Control during Water-alternating-CO<sub>2</sub> Flooding. Elsevier Inc., Amsterdam. 291, 120-171.
- [29]. Mao, L., Cai, M., Liu, Q., & Wang, G. (2021). Dynamical Simulation of High-Pressure Gas Kick in Ultra-Deepwater Riserless Drilling. *Journal of Energy Resources Technology*. 143(6), 15-31.
- [30]. Masoud, H. (2011). Application of Cause-and-Effect Diagram in the Oil Industry in Iran: A Case of Four Liter OilCanning Process of Sepahan Oil Company. *African Journal of BusinessManagement*. 5(26), 10900-10907.
- [31]. Michael, R. (1985). Use of Associated Gas in Petroleum Exporting Country: An Optimal Model. *Encostar*. 6(2), 1-38.
- [32]. Mikolajková, M., Saxén, H., & Pettersson, F. (2018). Linearization of an MINLP Model and its Application to Gas Distribution Optimization. Elsevier Inc., Amsterdam. 146, 156-168.
- [33]. Osesa, O. C., Ubani, C. E., Ifeme, B. U., & Okon, O. E. (2019). Gaslift Optimization to Improve Well Performance: A Case Study of X Field in Niger Delta. *International Journal of Science and Engineering Investigations*. 8(86), 115-119.
- [34]. Pengju, W. (2003). Development and Applications of Production Optimization Techniques for Petroleum Fields. A Dissertation Submitted to the Department of Petroleum Engineering, Stanford University.
- [35]. Processing Natural Gas (2019). Retrieved March 20th 2020, from [www.naturalgas.org/naturalgas/processing-ng](http://www.naturalgas.org/naturalgas/processing-ng)
- [36]. Rashid, K., Balley W., & Collet B. (2012). A Survey of Methods for Gas-Lift Optimization. *Modelling and Simulation in Engineering*. 5(7), 1-16.
- [37]. Rasouli, H., Rashidi, F., Karimi, B., & Khamehchi, E. (2014) A Surrogate Integrated Production Modeling Approach to Long-Term Gas-Lift Allocation Optimization. *Chemical Engineering Communications Journal*. 202, 647-654.
- [38]. Rios-Mercado, R.Z., & Borraz-Sanchez, C. (2014). Optimization Problems in Natural Gas Transportation Systems: A-State-of-The-Art-Review. *Applied Energy*. 147(9), 536-555.
- [39]. Runhua, T., Guazhong C., & Ruihong, Z. (2003). The Function Model of Existing Product Using Reverse Fishbone Diagram. *The Triz Journal*. 22(7), 16-21.
- [40]. Saeid, W. A.P., & John, Y.M. (2015). *Handbook of Natural Gas Transmission and Processing: Principles and Process*. 3<sup>rd</sup> Edition. Houston, Texas. Gulf Professional Publishing. 123-135.
- [41]. Sienz, J., & Innocente, M. S. (2008). Particle Swarm Optimization: Fundamental Study and its Application to Optimization and to Jetty Scheduling Problems. *Trends in Engineering Computational Technology*. 3(7), 14-16.
- [42]. Skorov, Y., Reshetnyk, V., Bentley, M., Rezac, L., Agarwal, J., & Blum, J. (2021). The Effect of Varying Porosity and Inhomogeneities of the Surface Dust Layer on the Modelling of Comet Gas Production. *Monthly Notices of the Royal Astronomical Society*. 501(2), 2635-2646.
- [43]. Srinivas, J. (2015). Review of Some Constrained Optimization Schemes. *Optimization for Engineering Problems*. ISTE Ltd and John Wiley & Sons Inc., Hoboken, New Jersey. 1-15.
- [44]. Stauffer, (2014), Recovering Natural Gas at Oil Wells. MITEL. Retrieved February 23<sup>rd</sup> 2021, from [www.energy.mit.edu/news/recovering-natural-gas-at-oil-wells](http://www.energy.mit.edu/news/recovering-natural-gas-at-oil-wells)
- [45]. Steinbach, M. C. (2007). On PDE Solution in Transient Optimization of Gas Networks. *Journal of Computational and Applied Mathematics*. 203(2), 345-361.
- [46]. Sun, Y. F., Zhong, J. R., Chen, G. J., Cao, B. J., Li, R., & Chen, D. Y. (2021). A New Approach to Efficient and Safe Gas Production from Unsealed Marine Hydrate Deposits. *Applied Energy*. 282(7), 116-259.
- [47]. Sunil, R. (2017). Introductory Guide on Linear Programming For (Aspiring) Data Scientist. Retrieved February 24<sup>th</sup> 2021, from [Analyticsvidhya.com/blog/2017/02/introductory-guide-on-linear-programming-explained-in-sample-english](https://analyticsvidhya.com/blog/2017/02/introductory-guide-on-linear-programming-explained-in-sample-english).
- [48]. Total (2019) Nigeria: Total Starts up Production -The Giant EginaField. Retrieved August 18<sup>th</sup> 2020, from <https://www.totalenergies.com/news>
- [49]. U.S. Energy Information Administration (2019). Petroleum and Other Liquids: U.S. Oil and Natural Gas Wells by Production Tale. Retrieved February 23<sup>rd</sup> 2021, from [www.eia.gov](http://www.eia.gov)
- [50]. Ullah, I., & Kim, D. (2018). An Optimization Scheme for Water Pump Control in Smart Fish Farm with Efficient Energy Consumption. *Processes*. 6(6), 65-69.
- [51]. Vanadzina, E., Gore, O., Viljainen, S., & Tynkkynen, V.P. (2014). Electricity Production as an Effective Solution for Associated Gas Utilization in the Reformed Russian Electricity Market. 12<sup>th</sup> International Conference on the European Energy Market (EEM), 1-5.
- [52]. Wang, P., Litvak, M., & Aziz, K. (2003). Optimization Production Operations in Petroleum Field. *Journal of Petroleum Technology*. 7(3), 22-27.
- [53]. Xue, L., Liu, Y., Xiong, Y., Liu, Y., Cui, X., & Lei, G. (2021). A Data-Driven Shale Gas Production Forecasting Method Based on The Multi-Objective Random Forest Regression. *Journal of Petroleum Science and Engineering*. 196(3), 107-108.
- [54]. Yaser, Q., Kerdphol, T., & Mitani, Y. (2015). Different Optimization Scheme for Community-Based Energy Storage System. International Conference on Electric Power and Energy Conversion Systems (EPECS). Sharjah, United Arab Emirate. 1-5.
- [55]. Zhang, Y., Liu, W., Huang, Z., Zheng, F., Le, J., & Zhu, S. (2021). Distributionally Robust Coordination Optimization Scheduling for Electricity-Gas-Transportation Coupled System Considering Multiple Uncertainties. *Renewable Energy*. 163(11), 2037-2052.
- [56]. Zheng, Q.P., Rebennack S., Iliadis N.A & Pardolos P.M (2010). Optimization Models in the Natural Gas Industry. *Handbook from Power Systems*. 121-148.